

## BAB I

### PENUTUP

Solusi sistem persamaan diferensial *fractional*

$$D^\alpha \mathbf{x}(t) = A\mathbf{x}(t) + B\mathbf{u}(t), \quad \mathbf{x}(0) = \mathbf{x}_0$$

dimana  $A \in \mathbb{R}^{n \times n}$ ,  $B \in \mathbb{R}^{n \times m}$ ,  $\mathbf{x}(t) \in \mathbb{R}^n$ ,  $\mathbf{u}(t) \in \mathbb{R}^m$  dan  $D\mathbf{x}(t)$  menyatakan turunan pertama dari  $\mathbf{x}$  terhadap  $t$ , dengan  $j - 1 < \alpha < j$ ,  $j \in \mathbb{N}$  adalah

$$\mathbf{x}(t) = \sum_{l=1}^j \Phi_l(t) \mathbf{x}^{(\alpha-l)}(0) + \int_0^t \Phi(t-\tau) B\mathbf{u}(\tau) d\tau$$

dimana

$$\Phi_l(t) = \sum_{k=0}^{\infty} A^k \mathcal{L}^{-1} [s^{-(k+1)\alpha+l+1}] = \sum_{k=0}^{\infty} \frac{A^k t^{(k+1)\alpha-l}}{\Gamma[(k+l)\alpha - l + 1]},$$

